

such that

$$\left| \int_a^b f(x) dx - \sum_{i=1}^n f(x_i^*) \Delta x \right| < \epsilon$$

for every $n > N$ and for every choice x_i^* in $[x_{i-1}, x_i]$